# **Postgraduate Department of Mathematics**

## **M.Sc.** Mathematics

#### **Programme Outcomes**

| PO1 | Acquire a deep sense of Mathematical, Logical and Analytical thinking                             |
|-----|---|
| PO2 | Create a strong base in theoretical methodologies   |
| PO3 | Explore new areas in applications of Mathematics.   |
| PO4 | Generate research aptitude and culture that leads to new theories.                                |
| PO5 | Ability to create mathematical models of real world situations and finding sustainable solutions. |
| PO6 | Develop scientific temper and integrity that ensures possible contributions to the subject        |
| PO7 | Become intellectually competent and to become a human being committed to development of society   |

#### **Programme Specific Outcomes**

| PSO1 | Acquire real insight into Advanced Mathematics.  |
|------|--|
| PSO2 | Build up a strong foundation in classical areas like Analysis, Abstract Algebra, and Measure theory. |
| PSO3 | Create interest and confidence to pursue higher studies in Mathematics.                              |
| PSO4 | Inculcate research aptitude among students.  |
| PSO5 | Understand different areas of Applied Mathematics.   |
| PSO6 | Develop Mathematical models of real-world problems and their solutions.                              |

#### **Course Outcomes**

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| SEN | SEMESTER 1        |                     |     |   |  |  |  |
|-----|-------------------|---------------------|-----|---|--|--|--|
|     |                   | Abstract<br>Algebra | CO1 | Analyze the structure of finitely generated abelian groups and factor groups.   |  |  |  |
| 1   | ME010101          |                     | CO2 | Apply Group Theory to problems in Combinatorics and other areas.  |  |  |  |
|     |                   |                     | CO3 | Apply Sylow's theorems and isomorphism theorems.  |  |  |  |
|     |                   |                     | CO4 | Apply the concepts of rings and ideals in polynomial factorization.   |  |  |  |
|     |                   |                     | CO1 | Analyze the theory of Vector spaces   |  |  |  |
|     |                   | Linear<br>Algebra   | CO2 | Understand the algebra of linear transformations and linear functionals.  |  |  |  |
| 2   | ME010102          |                     | CO3 | Apply the properties of determinants  |  |  |  |
|     |                   |                     | CO4 | Apply elementary canonical forms, characteristic values and annihilating polynomials.   |  |  |  |
|     |                   | Basic<br>Topology   | CO1 | Understand various types of topological spaces.   |  |  |  |
| 3   | <b>3</b> ME010103 |                     | CO2 | Analyze topological spaces using some basic<br>concepts like neighborhoods, interiors, accumulation<br>points and continuity. |  |  |  |
|     |                   |                     | CO3 | Applying the concept of connectedness in various topological spaces   |  |  |  |
|     |                   |                     | CO4 | Understand the hierarchy of separation axioms.  |  |  |  |
| 4   | ME010104          | Real Analysis       | CO1 | Analyze functions of bounded variation and rectifiable curves.  |  |  |  |
|     |                   | iten / indiyolo     | CO2 | Evaluate Riemann - Stieltjes integrability of   |  |  |  |

|   |          |              |     | functions   |
|---|----------|--------------|-----|---|
|   |          |              | 002 | Evaluate uniform convergence of Sequence and        |
|   |          |              | CO3 | Series of Functions                                 |
|   |          |              | CO4 | Analyze some special functions of real variables    |
|   |          |              | CO1 | Understand basic concepts and properties of graphs. |
|   |          |              | CO2 | Apply the concept of Connectivity and theorems on   |
|   |          |              |     | Trees to solve everyday life problems.              |
| 5 | ME010105 | Graph Theory | CO3 | Analyze vertex coloring and face coloring.          |
|   |          |              | CO4 | Analyze plane graphs and Dual of plane graphs.      |
|   |          |              |     |   |

#### **SEMESTER 2**

|   |          |                      | CO1 | Apply the concepts of extension fields to geometric constructions.   |  |  |  |
|---|----------|----------------------|-----|--|--|--|--|
|   | ME010201 | Advanced<br>Abstract | CO2 | Apply the concept of division algorithm in integral domains.   |  |  |  |
| 6 | ME010201 | Algebra              | CO3 | Apply field extension to polynomial factorization.   |  |  |  |
|   |          |                      | CO4 | Analyze the structure of groups and fields using Galois theory.  |  |  |  |
|   |          |                      | CO1 | Understand and apply the Urysohn Characterization<br>of normality and Tietze Characterization of normality |  |  |  |
| 7 | ME010202 | Advanced<br>Topology | CO2 | Apply the various topological properties on product spaces.  |  |  |  |
|   |          |                      | CO3 | Understand and apply embedding lemma, Tychonoff<br>Embedding and The UrysohnMetrisation Theorem            |  |  |  |
|   |          |                      | CO4 | Understanding the concept of Net , its convergence<br>and familiarize the idea of Homotopy of paths.       |  |  |  |
|   |          |                      | CO1 | Understand Symbols and Symbolic Operations in<br>Python  |  |  |  |
|   |          | Numerical            | CO2 | Apply the techniques of differentiation and  |  |  |  |

| 8  | ME010203                       | Analysis with |     | integration to solve problems   |
|----|--------------------------------|---------------|-----|---|
|    |                                | Python        | CO3 | Create Program to verify the continuity of a function<br>at a point, area between two curves and finding the<br>length of a curve |
|    |                                |               | CO4 | Apply Gauss Elimination Method, Doolittle's<br>Decomposition Method to solve problems   |
|    |                                |               | CO1 | Understand Riemann Sphere and Stereographic projection  |
|    |                                |               | CO2 | Apply theorems on convergence of the power series   |
| 9  | 9 ME010204 Complex<br>Analysis | -             | CO3 | Analyze problems related to analytic functions in<br>regions, conformal mappings and linear<br>transformations                    |
|    |                                |               | CO4 | Apply the theory and techniques of complex integration  |
| 10 | ME010205                       | Measure       | CO1 | Evaluate Lebesgue outer measure and Lebesgue measurability of sets  |
| 10 | Theory and<br>Integration      | •             | CO2 | Analyze the concept of Lebesgue measurability of functions and Lebesgue Integrals   |
|    |                                |               | CO3 | Apply the concepts of Integration over General<br>Measure Space   |
|    |                                |               | CO4 | Understand Product measure and related theorems   |

#### SEMESTER 3

| 11 | ME010301 | Advanced<br>Complex<br>Analysis | CO1<br>CO2<br>CO3<br>CO4 | Analyze Harmonic Functions and its basic properties<br>Understand and apply the Mean-Value Property,<br>Poisson's Formula, Schwarz's theorem and the<br>Reflection Principle<br>Understand the Riemann Zeta Function and its<br>properties.<br>Understand the Riemann Mapping Theorem,<br>Boundary behaviour and the Reflection Principle |
|----|----------|---------------------------------|--------------------------|---|
| 12 | ME010302 | Partial                         | CO1                      | Apply methods of solution for differential equations.   |

|    |             | Differential                 |     | Apply methods of solution for linear and nonlinear  |
|----|-------------|------------------------------|-----|---|
|    |             | Equations                    | CO2 | partial differential equations.   |
|    |             |                              | CO3 | Analyze various types of partial differential equations.  |
|    |             |                              | CO4 | Analyze solutions of Laplace equations and apply<br>Logarithmic potential to theory of functions.                           |
|    |             |                              | CO1 | Understand integral transforms and with special focus on Fourier Transforms   |
|    |             | Multivariate<br>Calculus and | CO2 | Analyze differentiability of multivariate functions   |
| 13 | 13 ME010303 | Integral<br>Transforms       | CO3 | Apply the concepts of higher order derivatives and finding extrema of functions   |
|    |             |                              | CO4 | Understand differentiation in higher dimensions and differential forms  |
|    |             |                              | CO1 | Analyze Normed Spaces and their properties.   |
|    |             | Functional<br>Analysis       | CO2 | Analyze Linear Operators, Bounded and Continuous<br>Linear Operators and Linear Functionals                                 |
| 14 | ME010304    |                              | CO3 | Analyze Inner Product Space, Hilbert space and further properties.  |
|    |             |                              | CO4 | Understand Zorn's lemma, Hahn-Banach theorem,<br>Hahn-Banach theorem for Complex Vector Spaces                              |
|    |             |                              | CO1 | and Normed Spaces<br>Apply different simplex methods to optimize linear<br>programming problems                             |
| 15 | ME010305    | Optimization<br>Techniques   | CO2 | Evaluate cutting plane method and branch and<br>bound method for optimizing general integer linear<br>programming problems. |
|    |             |                              | CO3 | Apply the concept of Networks in optimization.  |
|    |             |                              | CO4 | Apply algorithms to optimize non-linear   |
|    |             |                              |     | programming problems.   |

| SEN | SEIVIESIER 4 |                              |     |   |  |  |  |
|-----|--------------|------------------------------|-----|---|--|--|--|
|     |              | Spectral                     | CO1 | Apply category theorem and Uniform Boundedness theorem  |  |  |  |
|     |              |                              | CO2 | Analyze Open Mapping Theorem and Closed Graph<br>Theorem  |  |  |  |
| 16  | ME010401     | Theory                       | CO3 | Understand compact Linear Operators on Normed spaces and their spectral properties  |  |  |  |
|     |              |                              | CO4 | Understand Spectral Properties of Bounded Self<br>adjoint linear operators  |  |  |  |
|     | ME010402     | Analytic<br>Number<br>Theory | CO1 | Understand various arithmetic functions   |  |  |  |
|     |              |                              | CO2 | Understand some elementary theorems on the distribution of prime numbers.   |  |  |  |
| 17  |              |                              | CO3 | Applying the concept of congruence by using the Euler-Fermat theorem, the Lagrange's theorem and the Chinese remainder theorem. |  |  |  |
|     |              |                              | CO4 | Analyze the relationship between primitive roots and quadratic residues.  |  |  |  |

### **Elective Courses**

| SEMESTER 4 |          |                          |             |  |  |  |
|------------|----------|--------------------------|-------------|--|--|--|
|            |          |                          | CO1         | Apply the basics of Differential Geometry.           |  |  |
| 1          | ME800401 | Differential<br>Geometry | CO2         | Analyze Gauss map, geodesics and parallel transport. |  |  |
|            |          |                          | <b>CO</b> 2 | Apply the theory of Weingarten map, curvature of     |  |  |
|            |          |                          | CO3         | plane curves and surfaces, arc length and line       |  |  |

|   |          |                                |     | integrals   |
|---|----------|--------------------------------|-----|---|
|   |          |                                | CO4 | Understanding the theory of differential geometry in    |
|   |          |                                | 001 | higher dimensions.                                      |
| 2 | ME800402 | Algorithmic<br>Graph<br>Theory | CO1 | Evaluate Algorithms and its complexity to develop a     |
|   |          |                                |     | feel for the concept of an efficient algorithm.         |
|   |          |                                | CO2 | Apply basic properties of trees and their usefulness in |
|   |          |                                |     | algorithmic techniques.                                 |
|   |          |                                | CO3 | Evaluate concepts of Networks in max-flow min-cut       |
|   |          |                                |     | algorithm   |
|   |          |                                | CO4 | Analyze matchings and factorizations of graphs.         |
|   |          |                                | 04  |   |
| 3 | ME800403 | Combinatorics                  | CO1 | Apply algebraic concepts to solve basic problems in     |
|   |          |                                |     | real life using permutations and combinations           |
|   |          |                                | CO2 | Analyze Ramsey type problems and Ramsey                 |
|   |          |                                |     | numbers   |
|   |          |                                | CO3 | Apply the Generalized Principle of Inclusion and        |
|   |          |                                |     | Exclusion to solve real life problems.                  |
|   |          |                                | CO4 | Understand generating functions and recurrence          |
|   |          |                                |     | relations.  |